## LESSON SCENARIO 03: THE EGYPTIAN FRACTIONS

Topic: Fractions

Level: Age 14-18


Foreknowledge: Use fractions - simplification

Correlation: History, Geography

## LEARNING OUTCOMES

- Calculation with Egyptian fractions
- Write in hieroglyphs


## TEACHING METHODS

- Practical work
- Hands-on activity


## KEY WORDS

- Fraction
- History
- Calcul
- Egypt


## RESOURCES

- Pencil
- Paper


## ACTIVITIES

## INTRODUCTION TO THE EGYPTIAN NUMERATION (20 minutes)

## EXERCISE 1:

The teacher explains how Egyptians calculated. It can be recalled what a natural number and a fraction are.

In ancient times, the Egyptians calculated with natural numbers and fractions.
Regarding fractions, they only used $\frac{2}{3}$ and unit fractions, i.e. the inverses of integers (for instance, the inverse of 4 is $\frac{1}{4}$ ).

A discussion can follow on what hieroglyphs are and where they can be found: the teacher can show some photos.

In Ancient Egypt the two first writing systems were the Hieroglyphic (from about 3200 B.C.) and Hieratic scripts; the last one was a cursive script derived from Hieroglyphs, which was used by scribes, while Hieroglyphic script became largely restricted to monumental inscriptions.


HIEROGLYPHS ON THE TEMPLE OF KÔM OMBO.


## Worksheet for students:

The teacher can discuss the historical theme; then he/she explains how the Egyptians wrote numbers and gives instructions on what to do.

The numbering system was decimal and additive: each power of 10 was represented by a specific sign, as can be seen in the table below.

| Powers of <br> ten (decimal <br> writing) | 1 | 10 | 100 | 1000 | 10000 | 100000 | 1000000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| powers of <br> ten <br> (hieroglyphic <br> writing) |  |  |  |  |  |  |  |

For instance, 213 is represented by:

## © $\cap 11$

There is no strict rule for the arrangement of the numerical signs.
To represent $\frac{1}{n}$, we represent n and add a sort of oval somewhere which denotes the inverse. It can be seen above in the picture on the right.

Write these fractions in hieroglyphs:

$\frac{1}{36}:$
$\bigcirc 1111$
คกคI
$\frac{1}{1532}$ :

## ก○○ I I@

The teacher supervises the classroom and notices various ideas that students have explored and written down.

THE MAIN PART (10 minutes)

EXERCISE 2: The Eye of Horus

The teacher divides the students into groups of 2 or 3 . Then he/she gives instructions on what to do:


In Egyptian mythology, Seth (the god of violence) snatched an eye from his nephew Horus (the falcon-headed god). He divided it into 6 pieces and threw them into the Nile. This eye is called Oudjat.

The six pieces are:

- The left side of the eye $\frac{1}{2}$
- The pupil $\frac{1}{4}$
- The right side of the eye $\frac{1}{16}$
- The eyebrow $\frac{1}{8}$
- the teardrop $\frac{1}{64}$
- The curved tail $\frac{1}{32}$.

It is said that Thot (human God) restored the eye, symbol of good against evil, but the sum of these parts is not equal to 1 (the whole eye). He granted the missing part to any scribe seeking and accepting his protection.

Calculate the sum A of the fractions of the Oudjat and give the missing part!

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A=\frac{1}{2}+\frac{1}{4}+\frac{1}{16}+\frac{1}{8}+\frac{1}{64}+\frac{1}{32}=\frac{32}{64}+\frac{16}{64}+\frac{4}{64}+\frac{8}{64}+\frac{1}{64}+\frac{2}{64}=\frac{63}{64}
$$

The missing part $=\frac{64}{64}-\frac{63}{64}$

$$
=\frac{1}{64}
$$

TO GO FURTHER (10 minutes)

## EXERCISE 3:

Each student can work in autonomy. The teacher gives instructions on what to do:
The Egyptians expressed fractions by combining the unit fractions $\frac{1}{n}$ and $\frac{2}{3^{\prime}}$, all different ones.

If it is necessary, multiply numerator and denominator by 2 , then complete the calculation to obtain a sum of distinct Egyptian fractions.

First, we recommend to multiply by 2 the numerator and the denominator of the following fractions. Each fraction being greater than $\frac{1}{2}$, it is equal to $\frac{1}{2}+$ ?.
$\frac{6}{11}=\frac{12}{22}=\frac{11}{22}+\frac{1}{22}=\frac{1}{2}+\frac{1}{22}$
$\frac{5}{9}=\frac{10}{18}=\frac{9}{18}+\frac{1}{18}=\frac{1}{2}+\frac{1}{18}$
$\frac{4}{5}=\frac{8}{10}=\frac{5}{10}+\frac{1}{10}+\frac{2}{10}=\frac{1}{2}+\frac{1}{10}+\frac{1}{5}$

Another example, more complicated. The teacher can remind that Egyptians also used the fraction $\frac{2}{3}$ and suggest to use it in the writing of the following fraction:
$\frac{25}{36}=\frac{24}{36}+\frac{1}{36}=\frac{2}{3}+\frac{1}{36}$

## EVALUATION

FINAL PART (5 minutes)

## 1. WHAT IS THE NAME OF THE SIGN USED TO WRITE

 NUMBERS ON MONUMENTS ?CAN I WRITE THE NUMBER 2051?
2. WHAT SORTS OF FRACTIONS WERE IN USE IN ANCIENT EGYPT?
3. CAN I WRITE A FRACTION

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4. CAN I WRITE AND REPRESENT ?
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1. What is the name of the signs used to write numbers on monuments? Can I write the number 2051?

The signs are called hieroglyphs

2. What sort of fractions were used in Ancient Egypt?

They only used unit fractions (inverses of natural numbers) and $2 / 3$
3. Can I write a fraction? $\frac{1}{307}$

4. Can I write and represent $\frac{7}{24}$ ?

$$
\frac{7}{24}=\frac{6}{24}+\frac{1}{24}=\frac{1}{4}+\frac{1}{24}
$$

## INCLUSIVENESS GUIDELINES

Every student is different and their needs for the material might vary. Below you will find several tips that could make mathematics lesson more inclusive for students who struggle with learning disorders.

- When giving assignments to classroom try to break them into small pieces of information. Avoid the double tasks in the instructions. Remember that in case of operations/exercises with multiple steps, it is critical to help learners decompose the steps.
- You can use checklists for your students to make sure they have done all the steps
- Make sure the font, line spacing, and alignment of your document is accessible for students with learning disorders. It is recommended to use a plain, evenly spaced sans serif font such as Arial and Comic Sans. Others: Verdana, Tahoma, Century Gothic and Trebuchet. Spacing should be 1.5 and try to avoid justification in the text.
- At the end of each activity, take some time to ask the students what they have learnt to acknowledge every step in their learning process
- Make sure that the material the students manipulate is easy enough to grasp
- While using different media (paper, computer and visual aids) choose different background than white which can be too bright for students with learning disorders. The best choice would be cream or soft pastel but try to test different colours to learn more about student's preference.
- To stimulate short and long-term memory prepare for all the students in the classroom an outline describing what they are going to learn on this lesson and finish it with a resume of what has been taught. In this way they will strengthen the ability to remember information.


## EXAMPLE:

1. Start every lesson with a short "CHECK-IN"

- Today, we will study the topic (name of the topic)
- I will tell you about: (name 3 keywords connected with the topic)
- Then I will present exercises: (name the exercises from the student book)
- Then we will do exercises (explain the way student will be working: ex. together with teacher / in pairs /individually)
- Once the exercises will be done [To continue]

2. Then finish lesson with a short "CHECK-OUT"

- During the lesson we learn about (topic of the lesson)
- The most important things were: (name 3 keywords connected with the topic)
- We were able to do... (tell about the work student done during the lesson)
- We will explore the topic next time when we will learn about (name the following topic)

It is a small adjustment that will take $5 \mathbf{~ m i n}$ from the lesson but can make a great difference in the way that the material will be remembered. Try to create this as a routine habit.

